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Cavity prediction in sand mould production applying the DISAMATIC process [☆]

Emil Hovad^{a,c}, Per Larsen^c, Jon Spangenberg^a, Jens H. Walther^{a,d}, Jesper Thorborg^{a,b}, Jesper H. Hattel^a

^a*Department of Mechanical Engineering, Technical University of Denmark (DTU), Denmark. Produktionstorvet, Building 425, DK-2800 Kgs., Lyngby, Denmark.*

^b*MAGMA Giessereitechnologie GmbH, Kackertstr. 11, 52072 Aachen, Germany*

^c*DISA Industries A/S, Højager 8, Høje Taastrup, 2630 Taastrup, Denmark*

^d*Computational Science and Engineering Laboratory, ETH Zurich, CH 8092, Switzerland*

Abstract

The sand shot in the DISAMATIC process is simulated by the discrete element method (DEM) taking into account the influence and coupling of the airflow with computational fluid dynamics (CFD). The DEM model is calibrated by a ring shear test, a sand pile experiment and a slump test. Subsequently, the DEM model is used to model the propagation of the green sand inside the mold chamber and the results are compared to experimental video footage. The chamber contains two cavities designed to quantify the deposited mass of green sand. The deposition of green sand in these two cavities is investigated with three cases of different air vent settings which control the ventilation of the chamber. These settings resulted in different air- and particle-velocities as well as different accumulated masses in the cavities, which were successfully simulated by the model.

Keywords: DISAMATIC process, Sand casting, Green sand, Granular flow, Discrete element method

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[☆]Fully documented templates are available in the elsarticle package on CTAN.

*Corresponding author: Emil Hovad

Email address: emilh@mek.dtu.dk (Emil Hovad)

1. Introduction

The DISAMATIC process [1] is a sand casting process applying green sand as the molding material [2, 3]. The DISAMATIC process is typically used in the automotive industry to produce molds for metal castings in order to manufacture e.g. brake disks, differential cases and steering knuckles.

The DISAMATIC moulding process has been used since the early 1960s. Compared to conventional green sand moulding processes, it has a vertical parting line. Furthermore, it is a flaskless process, meaning there are no boxes supporting the moulds. The DISAMATIC moulding process is very productive compared to other processes, as it can produce up to 555 moulds per hour. Additionally, it can produce parts with low tolerances. Due to its efficiency and accuracy it is widespread used within the automotive sector.

The ever-rising demands to casting quality, especially within the automotive sector, lead among other things to higher demands to the mould quality. To comply with the higher demands to the mould quality, simulation tools come in handy in the development work having to be done. Until now most of the development work has been based on experience and a trial and error approach as no commercial simulation tools have been available for simulating the combined flow of green sand and air. The lack of commercial available simulation tools is partly driven by lack of material data of the green sand needed to describe the flow. Hence determination of material data has been a major part of this study.

The green sand consists mostly of quartz sand mixed with coal dust, bentonite (active clay) and water, which coats the sand grains to form a cohesive granular material where the green sand flow-ability is affected by the amount of bentonite and water. In [4] a regression model was applied to determine the relationship between the input value of the sand mixture, i.e active clay, dead clay, water content to the related output values of compactability, compressive strength, spalling strength and permeability. These relationships were developed from a DISAMATIC foundry. The green sand flow-ability was investigated in [5], [6] and the fluidized viscosity of green sand was investigated in

[7]. In [6] it was suggested that the green sand can be investigated as an yield stress material and an analytical derivation based on the yield stress material with additional overpressure similar to the conditions when the sand enters the chamber was made in [8]. Tri-axial tests have also been performed on green sand in order to obtain the yield locus in [9]. Uni-axial compression tests were made for green sand and the stress-strain curves were analysed in [10]. Green sand was tested with a ring shear tester obtaining the yield locus and a sand pile experiment in [11].

DEM simulations of the ring shear tester have been performed in [12] where the particle shape, cohesion and static friction were investigated with respect to the resulting tangential pre-shear stress and the peak stress (yield stress). A sensitivity study was performed in [13] simulating a Schulze ring shear tester studying the effect of several material parameters on the resulting tangential pre-shear stress. The resulting tangential pre-shear stress relationship to the particle-particle static friction coefficient ($\mu_{s,p-p}$) was asymptotic up to the value of $\mu_{s,p-p} < 0.70$ and a linear dependence was found on the parameters rolling friction coefficient ($\mu_{r,p-p}$) and the Young's modulus. A DEM adhesive elasto-plastic contact model was used to simulate uni-axial consolidation followed by unconfined compression to failure in [14].

A simulation of the sand casting process with a two phase continuum model has earlier been presented in [15] and continuum models have been designed to model granular materials as e.g. in [16, 17]. In [18] a multiphase model was applied to simulate a core shooting process numerically in 2-D and 3-D dimensions. The DISAMATIC process was first studied with a 2-D DEM model in [19] where the granular flow was compared to video footage. This study focused on the deflection of the sand flow causing "shadow effects" around the ribs placed in the geometry of the mould. The model applied a constant particle inlet velocity and particle diameters of 2 mm and 4 mm as representative sand particle clusters for the granular flow. In [11] the same geometry was investigated with a 2-D and 3-D DEM slice model applying the representative particle cluster diameter of 2 mm. A 2-D sensitivity study was performed with respect

to the particle-wall interaction which showed the particle-wall values to be of less importance for the flow behaviour and filling times than e.g. particle inlet velocity. The DEM model was calibrated from experiments (ring shear test and sand pile experiment) and afterwards a velocity function for the granular flow was found from video footage.

In this study the framework of [11] is applied for calibrating the DEM model using a ring shear tester to obtain the static friction coefficients and a sand pile experiment for calibrating the rolling resistance and cohesion value for the particle-particle interaction. Additionally the mass of the DEM particle is recalculated and a slump experiment is used for calibrating the rolling resistance for the particle-wall interaction. Finally a DEM model and a CFD-DEM model are tested by simulating the flow and deposition of green sand in the two cavities and subsequently compared to the experimental observations for the three cases of the air vent settings.

2. Governing equations

2.1. Granular flow: Discrete element method

The framework of [11] is applied in this work where the commercially available software of STAR-CCM+ [20] is used for simulating the DISAMATIC process.

2.1.1. Contact notation

The notation for the particle contact is from [21], where particle i and particle j in contact are denoted by their respective positions at $\{\vec{r}_i, \vec{r}_j\}$, the velocities $\{\vec{v}_i, \vec{v}_j\}$, the angular velocities of $\{\vec{\omega}_i, \vec{\omega}_j\}$ and the distance between the two particles is denoted $r_{ij} = \|\vec{r}_i - \vec{r}_j\|_2$. The position vector from particle j to i is $\vec{r}_{ij} = \vec{r}_i - \vec{r}_j$ and the normal overlap $\delta_{ij} = (R_i + R_j) - r_{ij} = 2R$ with a uniform radius of R for all the particles.

2.1.2. Normal contact force

The normal force on particle i from particle j can be found as,

$$\vec{F}_{n_{ij}} = \vec{n}_{ij} k_n \delta_{ij}^{\frac{3}{2}} - N_{n_{ij}} \vec{v}_{n_{ij}} + \vec{F}_{coh_{ij}} \quad (1)$$

$\vec{n}_{ij} = \frac{\vec{r}_{ij}}{r_{ij}}$ is the unit normal vector, $\vec{v}_{n_{ij}}$ is the relative normal velocity and δ_{ij} is the normal overlap. $N_{n_{ij}}$ is the normal non-linear damping coefficient, $F_{coh_{ij}}$ is the cohesion, K_n is the stiffness in the normal direction, $N_{n_{ij}}$ is the damping in the normal direction, for further details see [11]. The particle-particle constant cohesion force in the normal direction is,

$$\vec{F}_{coh_{ij}} = -1.5\pi R_{min} W \vec{n}_{ij} \quad (2)$$

$R_{min} = R$ is the minimum radius of contact, W is the cohesion parameter. The cohesion $\vec{F}_{coh_{ij}}$ selected is the Johnson-Kendall-Roberts (JKR) model from [22] with the factor of -1.5.

2.1.3. Tangential contact force

The tangential force on particle i from particle j can be found as,

$$\vec{F}_{t_{ij}} = K_t \frac{\vec{t}_{ij}}{\|\vec{t}_{ij}\|_2} \delta_{t_{ij}}^{\frac{3}{2}} - N_{t_{ij}} \vec{v}_{t_{ij}} + \vec{T}_{rol_{ij}} \quad (3)$$

\vec{t}_{ij} is the tangential direction of the overlap, $\delta_{t_{ij}}$ is the tangential overlap, K_t is the tangential stiffness, G_{eq} is the equivalent shear modulus, $N_{t_{ij}}$ is the tangential non-linear damping coefficient. The rolling resistance for the particle-particle interaction used is the constant torque method defined as,

$$\vec{T}_{rol_{ij}} = -\frac{\omega_{rel}}{|\omega_{rel}|} \mu_r R_{eq} |\vec{F}_{n_{ij}}| \quad (4)$$

The relative angular velocity between the two particles is defined as $\vec{\omega}_{rel} = \vec{\omega}_i - \vec{\omega}_j$ and the torque from the rolling resistance is $\vec{T}_{rol_{ij}}$.

Note that there is a maximal tangential force due to Coulomb's law,

$$\|\mu_s \vec{F}_{n_{ij}}\|_2 < \|\vec{F}_{t_{ij}}\|_2 \quad (5)$$

the particle-particle static friction coefficient is denoted $\mu_{s,p-p}$ and particle-wall static friction coefficient is denoted $\mu_{s,p-w}$.

2.1.4. Summing the forces

The total resultant force on particle i is then computed by summing the contributions of all particles j with which it currently interacts, thus:

$$\vec{F}_i^{tot} = m_i \vec{g} + \sum_j \left(\vec{F}_{n_{ij}} + \vec{F}_{t_{ij}} \right) \quad (6)$$

where \vec{g} is the acceleration due to gravity. The total torque acting on particle i is given by

$$\vec{T}_i^{tot} = -R_i \sum_j \vec{n}_{ij} \times \vec{F}_{t_{ij}} \quad (7)$$

From these two expressions the acceleration, velocity, position and rotation, are calculated by Newton's second law, numerically for each time step.

2.2. Air flow: Navier Stokes equations

The low air pressures (P) measured in the chamber during the sand shot and the corresponding low air velocities (\mathbf{v}_g) make the assumption of the air phase being an incompressible fluid valid for small values of the Mach number ≤ 0.3 . Then the continuity equation becomes,

$$\rho_g \frac{\partial}{\partial t} (\epsilon_g) + \rho_g \nabla \cdot (\epsilon_g \mathbf{v}_g) = 0 \quad (8)$$

where ϵ_g is the air volume fraction found from $\epsilon_g = \frac{V_g}{V_g + V_s}$ where V_g is the volume of the air phase and V_s is the volume of solid phase. Navier-Stokes equations for the incompressible air phase are,

$$\rho_g \frac{\partial}{\partial t} (\epsilon_g \mathbf{v}_g) + \rho_g \nabla \cdot (\epsilon_g \mathbf{v}_g \mathbf{v}_g) = -\epsilon_g \nabla P + \epsilon_g \rho_g \mathbf{g} - \nabla \cdot (\epsilon_g \tau_g) - \mathbf{I}_f \quad (9)$$

where $\rho_g = 1.18415 \frac{\text{kg}}{\text{m}^3}$ is the density of the air phase, $\mathbf{g} = [0, -9.82, 0] \frac{\text{m}}{\text{s}^2}$ is gravity and the shear stress on the air is τ_g where the air is assumed to be a Newtonian fluid with the dynamic viscosity of $\mu = 1.85508 \times 10^{-5} \text{ Pa} \cdot \text{s}$. The two-way coupling between the air phase and the solid phase is enforced via the inter-phase momentum transfer of \mathbf{I}_f due to the drag on the solid phase.

2.3. The inter-phase momentum transfer

A source smoothing method is applied for the inter-phase momentum transfer of \mathbf{I}_f which averages the momentum transfer from larger parts of the mesh to the solid phase stabilizing the simulations to ensure converging simulations. The drag force on the solid phase is,

$$\mathbf{F}_D = -\frac{1}{8}\pi d^2 \rho_g C_d (\mathbf{v}_g - \mathbf{u}) |\mathbf{v}_g - \mathbf{u}| \quad (10)$$

where \mathbf{u} is the velocity of the solid phase and d is the diameter of the particle. The interaction of the solid phase with the air phase is described by the Schiller-Naumann drag model,

$$C_d(Re_p) = \begin{cases} \frac{24}{Re_p} (1 + 0.15 Re_p^{0.687}), & Re_p \leq 10^3 \\ 0.44, & Re_p > 10^3 \end{cases} \quad (11)$$

where Re_p is the particle Reynolds number and it is defined as,

$$Re_p = \frac{\rho_g |\mathbf{v}_g - \mathbf{u}| d}{\mu} \quad (12)$$

where $|\mathbf{v}_g - \mathbf{u}|$ is the slip velocity.

2.4. Turbulence model

Modelling the air phase as a continuum is done by solving Navier Stokes equations with the finite volume method (FVM) applying a polyhedral mesh. The k- ϵ turbulence model is used and all the methods are described in [20].

3. The green sand tests and calibrating of the DEM model

The following green sand tests and calibrations of the DEM model are performed.

3.1. The water content test

The percentage of water content is found by heating a sample of green sand and measuring the mass of water which is lost. The details of the water content test also denoted the moisture determination is described in [3]. This is a standard test typically performed in a foundry.

3.2. The Schulze ring shear tester

The Schulze ring shear tester is applied for characterizing the flow of granular materials in order to obtain the yield locus and the wall yield locus. The test procedures can be found in [23, 24]. The particle-wall static friction coefficient ($\mu_{s,p-w}$) is acquired directly from the wall friction angle as demonstrated in [11]. The particle-particle static friction coefficient in the simulation is found directly from the linearized yield locus angle. The linearized yield locus angle is described in [11, 23, 24, 25].

3.3. The sand pile experiment and the DEM calibration.

The sand pile experiment is applied for characterizing and calibrating the DEM model with respect to the height of the sand pile (h_p) above the box cf. Fig. 1(left) and described in [11]. The parameters that are calibrated from the sand pile height are the particle-particle rolling resistance interaction ($\mu_{r,p-p}$) and the particle-particle cohesion value (W_{p-p}).

[Figure 1 about here.]

3.4. The compactability test

The compactability test described in [3, 11] is applied to characterize the green sand condition and this is the standard test performed in the foundries. The green sand is poured into the cylinder with a tube filler accessory, subsequently the mass is measured before the ramming and from this the loose density of the green sand ρ_{exp} is calculated cf. Fig. 1(middle). The compactability of the sand mixture is finally found by the rammer method described in [3]. The cylinder has a height of $H_{cyl} = 0.12$ m and a diameter of $D_{cyl} = 0.05$ m.

3.5. Scaling the DEM particle density

The preliminary density of the DEM particles (ρ_{DEM}^\dagger) used in the sand pile simulations (Fig. 1(left)) is corrected to ρ_{DEM}^* to obtain a correct simulated

bulk density (ρ_{sim}^*) equal to the loose density measured before the ramming (ρ_{exp}) cf. Fig. 1(middle)

$$\rho_{DEM}^* \approx \rho_{DEM}^\dagger \left(\frac{\rho_{exp}}{\rho_{sim}} \right). \quad (13)$$

Here ρ_{sim} denotes the preliminary bulk density obtained from the sand pile simulation. Thus the subsequent slump calibration has the correct simulated bulk density (ρ_{sim}^*) shown in Fig. 1(right).

3.6. The slump cylinder experiment and the DEM calibration

The slump cylinder experiment is performed by lifting the cylinder rapidly upwards emulating the instantaneous wall opening in the simulation to finally find the slump length. The cylinder applied for the slump test is the same as the cylinder applied in the compactability test. The slump cylinder experiment is shown in Fig. 2(top) and the slump simulation is shown in Fig. 2(bottom).

[Figure 2 about here.]

When the green sand slump has settled the two diameters orthogonal to each other (l_x, l_y) are measured and the average is calculated for the final slump length l_p where the simulated slump length is found in a similar way from the algorithm first applied in [26] and described in [25]. The rolling resistance of the particle-wall interaction $\mu_{r,p-w}$ is calibrated with respect to the slump length. The slump simulation is applying the values found from the earlier calibrations together with the re-calculated DEM particle density (ρ_{DEM}^*).

For a correct density in the slump simulation the number of initial injected particles are found from the re-calculated DEM particle density (ρ_{DEM}^*) together with the experimental loose density in the cylinder (ρ) in the following way,

$$N \approx \frac{\rho_{sim} H_{cyl} \frac{\pi}{4} D_{cyl}^2}{\rho_{DEM}^* \frac{\pi}{6} d^3} \quad (14)$$

The particle are initially placed on an initial lattice with an initial random velocity to ensure a random packing.

4. The experimental tests of the DISAMATIC process

4.1. The DISAMATIC process

The DISAMATIC process is illustrated with a special setup in the chamber shown in Fig. 3 with two cavities on the left hand side each having a narrow opening for testing the ability of green sand to enter the two cavities. During the sand shot the compressed air in the air tank drives the sand flow vertically down from the hopper through the sand slot into the chamber filling the mold chamber and the two cavities.

[Figure 3 about here.]

In the casting process the sand mold is squeezed also, but in this experiment the swing plate on the left hand side is opened instead and the green sand is then brushed out of the cavities so that the mass of the green sand in the cavities can be measured at the end of each experiment. The flow inside the chamber is captured with the video camera (v_1) placed on the right hand side on the chamber (Pressure plate: PP) and photos are shown in Fig. 4 for eight stages of the sand shot.

[Figure 4 about here.]

The red light shown in Fig. 4(a) indicates when the valve between the air tank and the hopper is activated, this moment is defined as $t_{start} = 0$. A very short time after the valve activation the air pressure over the sand in the hopper starts to increase. Later during the sand shot, the sand starts flowing into the chamber shown in Fig. 4(a) and this moment is denoted t_0 . Seven lines are marked to quantify the seven filling times $t_1 - t_7$, which is defined as when the green sand reaches the seven lines as shown in Fig. 4(b)-(h).

In Fig. 5 the flow in the cavities is captured with the mini video cameras v_2 and v_3 where the filling times of the cavities are monitored as t_1 when the sand enters the cavity and t_2 when the camera is blocked by the green sand. The times for the two cavities are denoted the following way: For the bottom cavity $t_{b,1}$ and $t_{b,2}$ and for the top cavity $t_{t,1}$ and $t_{t,2}$.

[Figure 5 about here.]

4.2. The two air vent types

Two types of air vents are applied for ventilating the chamber where one type is placed in the chamber (a_c) and another type is placed on the SP side inside the cavities (a_p). Experiments for the air vents flow rate versus pressure drop are shown for the air vent in the chamber in Fig. 6(blue line) and for the air vents on the pattern plate in Fig. 6(black line). The pattern plate air vents are placed in the cavities.

[Figure 6 about here.]

The physical behaviour shown in Fig. 6 resembles the Darcy flow,

$$Q = -a\Delta p \quad (15)$$

where Q is the air flow rate and ΔP is the pressure difference across the air vent and a is the permeability of the air vent. The chamber air vent type has the value of $a_c = 1.274 \times 10^{-6} \frac{\text{m}^3}{\text{sPa}}$ and the air vent type placed in the cavities on the pattern plate has the value of $a_p = 2.34 \times 10^{-6} \frac{\text{m}^3}{\text{sPa}}$.

4.3. The air vent settings and the three test cases

The air vents and their positions are illustrated in Fig. 7 where a total of 294 air vents are opened and this is denoted case 1. There are 238 air vents of the type a_c where 112 air vents are placed at the top of the PP chamber side, 52 air vents are placed at the top of the SP side shown in Fig. 7(Chamber top view) and 2×37 air vents are placed on the chamber sides in Fig. 7(Chamber side view). On the pattern plate shown in Fig. 7(Swing plate view) each cavity has 28 cavity air vents of the type (a_p) where the purpose of the air vents in the cavities is to ensure a better ventilation and thereby transporting a larger amount of green sand into the cavities.

[Figure 7 about here.]

The three cases of the air vents settings are investigated with 2.0 bar overpressure where the three air vent settings are presented in table 1. The three air vents settings are: case 1 with all the air vents opened, case 2 with all the air vents closed in the top of the SP side and 5 closed side air vents and finally case 3 with 14 air vents closed in each pattern plate.

[Table 1 about here.]

The chamber measurements without the pattern plate have the width $W = 0.50$ m, height $H = 0.48$ m and depth $D = 0.60$ m. The cavities in the pattern plate has the depth $D_c = 0.57$ m and is also centred at the middle of the chamber depth. The orifice opening height of the cavities are set to 0.015 m and the height of the cavities is $H_c = 0.085$ m. The sand slot has the width $W_i = 0.04$ m and a depth $D_s = 0.54$ m and is centred at the middle of the chamber depth. The encapsulation areas for the air vents A_p , A_{SP} , A_{PP} are applied for calculating the porous resistance for the simulations together with the two types of air vents in eq. 18.

5. Simulation settings for the DISAMATIC process

5.1. The simulated geometry

[Figure 8 about here.]

The flow is modelled as a 3-D slice placed in the middle of the chamber shown in Fig. 8 with a slice depth of $D_s = 0.01$ m in the z-direction where this direction has symmetry. Thereby the side air vents are not simulated due to the slice geometry of the simulation.

5.2. Boundary conditions for the granular flow

5.2.1. DEM particle flow rate

The chamber is divided into the eight different volumes ($V_1 - V_8$) where $V_n = A_n D_s$ and the sand jet is included in the first volume (V_1) and thereby excluded from the other volumes as shown in Fig. 8. The volumes are filled with

green sand at the subsequent filling times ($t_1 - t_7$). From this the flow rates are calculated ($f_1 - f_7$) where the flow rate for the last area A_8 is assumed to be equal to the flow rate of f_7 . The particle flow rate function $f_y(t)$ in the DEM simulations is calculated from the volumes of the chamber $V_1 - V_7$ (neglecting the cavities on the swing plate) multiplied with the maximum particle packing fraction of approximately $\eta_h = 0.74$ divided with the volume of the particle and the individual flow rate intervals $\Delta t_1 = t_1$, $\Delta t_2 = t_2 - t_1$, $\Delta t_3 = t_3 - t_2$ etc. in the following way,

$$f_n = \frac{V_n \eta_h}{\frac{\pi}{6} d^3 \Delta t_n} \quad (16)$$

Volume conservation for the number of injected particles is established in the transition zone from the flow rate of f_n to f_{n+1} with a linear interpolation in the time interval of $\Delta t_{n,s} = \min(\Delta t_n, \Delta t_{n+1})$. The slope of linear interpolation in the time interval is calculated as $s_n = \frac{f_{n+1} - f_n}{\Delta t_{n,s}}$ and the particle flow rate function $f_y(t)$ then becomes,

$$\begin{aligned} f_y(t) &= f_n & \text{if } t_{n-1} + \frac{\Delta t_{n-1,s}}{2} \leq t \leq t_n - \frac{\Delta t_{n,s}}{2} \\ f_y(t) &= f_n + \left(t - \left(t_n - \frac{\Delta t_{n,s}}{2} \right) \right) s_n & \text{if } t_n - \frac{\Delta t_{n,s}}{2} \leq t \leq t_n + \frac{\Delta t_{n,s}}{2} \end{aligned} \quad (17)$$

The calculated flow rate of $f_y(t)$ is applied for all the following DEM particle inlet velocities. The filling times applied for obtaining the flow rate are shown in Fig. 9 where the full lines represent the selected experiment used for simulating each of the three cases.

5.2.2. DEM particle inlet velocity

The time dependent inlet particle velocity ($v_y(t)$) in the vertical y -direction is obtained from the estimated velocities $v_n = \frac{A_n}{t_n W_i}$, where the seven areas ($A_1 - A_7$) are shown in Fig. 8. The transition from velocity v_n to v_{n+1} is found using eq. 17.

[Figure 9 about here.]

The filling times ($t_1 - t_7$) used for calculating the inlet velocity are shown in Fig. 9 for the selected experiments. The resulting time dependent velocities

$v_y(t)$ for three simulations are shown in Fig. 10(a) where the spikes are due to the video frame rate 60 frames/s making it difficult to exactly determine the filling times shown in Fig. 9. To smooth out the spikes a two stage time dependent inlet velocity $v_{2y}(t)$ is constructed, where v_1 and v_2 are connected by eq. 17. The first constant velocity is obtained as previously whereas the second constant velocity v_2 is chosen among the velocities $v_y(t > t_1)$ with the longest duration cf. Fig. 10(a). An exception is made in case 3, where the second longest time duration is chosen to avoid an otherwise unrealistic velocity. The two stage time dependent inlet velocities are shown in Fig. 10(b). Lastly, two constant particle velocities of $v_y(t) = -5 \frac{\text{m}}{\text{s}}$ and of $v_y(t) = -7 \frac{\text{m}}{\text{s}}$ are considered. For each of the three cases all the four different vertical velocities are simulated for both pure DEM simulations (vacuum) and CFD-DEM (including air phase) and this gives a total of 24 simulations.

[Figure 10 about here.]

A normal distribution is applied for the horizontal velocity to emulate the random nature of the green sand flow in the chamber and was originally applied in [11]. Thus, the horizontal velocity $v_x(t)$ has a mean of $0.0 \frac{\text{m}}{\text{s}}$ and a standard deviation $0.1 \frac{\text{m}}{\text{s}}$ and a maximum fluctuation of $\pm 1.0 \frac{\text{m}}{\text{s}}$ as in [11].

5.3. Boundary conditions for the air flow

5.3.1. Air inlet pressure

In this study the focus is on simulating the flow of air and green sand in the chamber, the air inlet pressure boundary for the chamber is placed at the sand slot where the green sand also enters, as shown in Fig. 11. The air pressure at the boundary is obtained from the top pressure sensor shown in Fig. 7(red circle).

5.3.2. Air outlets

A symmetry boundary is applied in the z -direction (depth direction) which resembles the conditions in the center of the mold during the sand shot and the

boundary is shown in Fig. 11. The mesh has a polyhedral structure with the cell size of $\Delta x = 0.025$ m giving the number of cells of around ≈ 9000 . There are 4 porous baffle interfaces in the chamber each having an elongated air channel with a pressure outlet set to 0 bar relative to the pressure of the inlet.

[Figure 11 about here.]

5.3.3. Air outlet: Darcy flow in the porous baffle

The DISAMATIC air vents from eq. 15 are set in parallel because the n air vents are positioned side by side in the areas (A),

$$\beta = \frac{A}{\rho_g a n} \quad (18)$$

β is the constant porous viscous resistance [20] and is determined by the air vent type (a), the number of air vents (n) over the cross sectional area (A) and the density of the fluid ρ_g . The placements and areas of the air vents are illustrated in Fig. 7 and for the simulation shown in Fig. 11. The outlet boundary settings for all the three cases are shown in table 2 where in case 2 and in case 3 a number of air vents are blocked and thereby the porous areas are changed together with β .

[Table 2 about here.]

5.4. Monitoring the simulated flow

The seven filling times $t_1 - t_7$ are monitored for the simulations and found from the particle filling of the seven volumes ($V_1 - V_7$). A volume V_n is filled when the minimum volume of particles V_p is above the packing fraction of 0.4 and thereby the filling time is monitored t_n .

The mass of the DEM particles in the cavities of the slice geometry D_s are monitored with respect to time and scaled with $\frac{D_c}{D_s} = 57$ due to the ratio of the simulated geometry depth D_s versus the experimental depth of the cavities D_c .

6. Results of the green sand tests and the calibrations

6.1. Results of the green sand tests

The result of particle-particle static friction coefficient and the particle-wall static friction coefficient from the ring shear test, the sand pile height, the green sand density, the slump length, the compactability and water content are shown in table 3.

[Table 3 about here.]

6.2. Calibration of the DEM model

6.2.1. General settings for all the DEM simulations

The radius of the DEM particle, coefficient of restitution, Poisson's ratio and Young's modulus are obtained the framework of [11] and listed in table 4. The particle-wall static friction coefficient applied in the simulation takes the value of $\mu_{s,p-w} = 0.33$ corresponding to the average value obtained from the ring shear tests for the green sand samples interaction with a stainless steel plate with the procedure described in [11]. The particle-particle static friction coefficient of $\mu_{s,p-p} = 0.57$ is obtained from the ring shear test's linearized yield locus angle, where all the parameters are listed in table 3.

[Table 4 about here.]

In the sand pile simulations it is assumed that the particle-wall rolling resistance is $\mu_{r,p-w} = 0.4$, this is a reasonable assumption based on prior simulations of the slump cylinder test. Note, that the particle-wall rolling resistance $\mu_{r,p-w}$ will be calibrated later in the slump cylinder simulation. The initial DEM particle density of $\rho_{DEM}^{\dagger} = 1750 \frac{\text{kg}}{\text{m}^3}$ is a reasonable assumption based on prior simulations of the sand pile density.

6.2.2. Results of the sand pile calibration

The experimental sand pile height is plotted together with the simulated sand pile heights in Fig. 12. The simulations with $\mu_{r,p-p} = 0.4$ and $W_{p-p} =$

$0.3 \frac{\text{J}}{\text{m}^2}$ (blue dotted line) and $\mu_{r,p-p} = 0.2$ and $W_{p-p} = 0.5 \frac{\text{J}}{\text{m}^2}$ (red dot) both give values of the height which are within the standard deviation of the measured height shown in Fig. 12. The selected parameters are $\mu_{r,p-p} = 0.4$ and $W_{p-p} = 0.3 \frac{\text{J}}{\text{m}^2}$ because they give a more conically shaped sand pile which was also observed in the experiments and described in [11].

[Figure 12 about here.]

6.2.3. Re-calculating the DEM particle density

In Fig. 13 the simulated sand pile density (ρ_{sim}) is compared to the experimental loose poured bulk density (ρ_{exp}) measured in the cylinder before the compactability test.

[Figure 13 about here.]

The chosen particle density for the sand pile simulation is $\rho_{DEM}^{\dagger} = 1750 \frac{\text{kg}}{\text{m}^3}$ which is too small for the selected h_p with the particle-particle value of $\mu_{r,p-p} = 0.4$ and $W_{p-p} = 0.3 \frac{\text{J}}{\text{m}^2}$ when compared to the bulk density measured in the cylinder. Therefore the density is re-calculated from eq. 13 which gives $\rho_{DEM}^* = 1900 \frac{\text{kg}}{\text{m}^3}$.

6.2.4. Results of the slump length simulation

The slump simulation is applied for determining the particle-wall rolling resistance $\mu_{r,p-w}$ with less than a standard deviation away from the the slump experiment l_p . The obtained values from the sand pile experiment of $\mu_{r,p-p} = 0.4$ and $W_{p-p} = 0.3 \frac{\text{J}}{\text{m}^2}$, the scaled DEM particle density of $\rho_{DEM}^* = 1900 \frac{\text{kg}}{\text{m}^3}$ and the number of particles injected into the cylinder which is found from eq. 3.6 are applied for the slump calibration.

[Figure 14 about here.]

The slump length result from the experiment is shown in Fig. 14 where the mean slump length l_p is the black diamond and the standard deviation is indicated by the two black horizontal lines. The particle-wall interaction of $\mu_{r,p-w} = 0.5$ is

below a standard deviation away from the average experimental slump length shown in Fig. 14.

6.2.5. Settings for the final simulations of the DISAMATIC process

The results from the calibration of the DEM model are listed in table 5 where the general simulation settings were presented in table 4.

[Table 5 about here.]

7. Results of the DISAMATIC process and simulations

7.1. Experimental air pressures measured from the sensors

For the selected sand shot in case 1, the measured air pressures can be seen as a function of time in Fig. 15. The air pressure builds up in the hopper (black line) in the start of the sand shot as the pressure decreases in the air tank (black dotted line) shown in Fig. 15. The pressure in the hopper starts to decrease after t_1 when the green sand has reached the bottom line l_1 of the chamber shown earlier in Fig. 4(b). The pressure decrease in the hopper is due to a equilibrium pressure is reached with the air tank and the air pressure now drops and the air flow propagates towards the chamber. In Fig. 15 the duration of time from t_0 to t_1 is longer than the subsequent next time intervals t_1 to t_2 etc. which is due to the larger pressure difference in the hopper versus the chamber. Video footage of the times $t_0 - t_7$ are shown in Fig. 4(a)-(h) for the selected sand shot in case 1. The filling times of the two cavities with the top cavity times $t_{t,1} - t_{t,2}$ (red) and the bottom cavity times $t_{b,1} - t_{b,2}$ (blue) are shown in Fig. 15.

[Figure 15 about here.]

The green sand starts entering the chamber at the monitored time of t_0 at this time the air pressure in the top of the chamber starts slowly to increase which is shown in Fig. 16 for the three selected cases. The air pressure in the top of the chamber shown in Fig. 16 is plotted from the time of t_0 where the green sand starts to enter the chamber, which is chosen to be the initial starting time for

the simulations. The three plotted pressures are applied as the sand slot inlet pressure in the CFD-DEM simulations with the minimum pressure of zero.

[Figure 16 about here.]

7.2. The filling times $t_0 - t_7$ of the chamber

The selected experimental and simulation filling times for case 1 are shown in Fig. 17 for the initial starting time of $t_0 = 0$.

[Figure 17 about here.]

The constant velocity of $7 \frac{\text{m}}{\text{s}}$ and $5 \frac{\text{m}}{\text{s}}$ have the shortest filling times in the initial part of the simulated sand shot $t_1 - t_4$ whereas the later filling times are too long $t_4 - t_7$. The filling times of the time dependent velocity $v_y(t)$ has the best agreement with the experiments and the two stage time dependent velocity function $v_{2y}(t)$ has the second best agreement with the experiment. The starting velocity of v_1 for both of the time dependent velocities were set too slow because the simulated filling time of t_1 was too long when compared to the experimental time shown in Fig. 17.

The filling times of the simulations and the selected experiment in case 1 are in good agreement with the other selected cases case 2 and case 3.

7.3. The sand deposited in the two cavities

[Table 6 about here.]

The deposited masses in the two cavities from the three cases and the selected experiments are listed in table 6. Considering all the experimental cases, case 2 showed the largest mass of deposited sand in both the top cavity and bottom cavity, being 1220 g and 933 g, respectively. As earlier mentioned one experiment was selected for simulation for each of the three cases considered.

The simulated masses in the two cavities are monitored with respect to time and compared to the selected experiment for the three cases shown in Fig. 18 - Fig. 20. For all the three cases of the CFD-DEM simulations the deposited

mass in the two cavities were overestimated when compared to the selected experiments. For case 3 the CFD-DEM simulations had better agreement with the selected experiment shown in Fig. 20 as compared to the other simulated cases.

[Figure 18 about here.]

[Figure 19 about here.]

For case 1 and case 2 the deposited mass in DEM simulations' for the two cavities are underestimated when compared to the selected experiments shown in Fig. 18 - Fig. 19, except for $v_y(t)$ in the top cavity shown in Fig. 19(b) plotted with the blue dotted line. In case 3 the DEM simulations has a good agreement with the selected experiment shown in Fig. 20, except for $v_y(t)$ in especially the top cavity which is shown in Fig. 20(b) which is due to the high particle velocity in the end of the simulation shown earlier in Fig. 10(a).

The inlet velocity for the DEM particles in the simulated sand shot was initially larger for the two constant inlet particle velocities as compared to the simulations with the time dependent velocities and thereby the particles entered earlier in the bottom cavity in all the three simulated cases with DEM.

[Figure 20 about here.]

7.4. The qualitative flow behaviour

The CFD-DEM simulated results of case 1 - 3 are shown in Fig. 21. The three simulations overestimated the mass in the cavities as when compared to the experiments and the DEM simulations. For the cases 1 and 2 simulated air velocities in the cavities were around $15 - 30 \frac{m}{s}$ as compared to case 3 where the cavity air velocities were around $10 - 20 \frac{m}{s}$. When comparing case 2 to both case 1 and case 3 in Fig. 21(middle figures) the particles have greater velocities and a more pronounced particle jet when the particles entered the bottom cavity. When comparing the simulations to the experiments shown in Fig. 21 all the simulations were in good agreement with the experiments with respect to the sand pile shape at the time $t=0.50$ s.

[Figure 21 about here.]

8. Conclusion

In the present paper the sand shot in the DISAMATIC process was investigated with three different air vent settings with respect to the mass of green sand deposited in two cavities, this investigation was performed experimentally as well as simulated. For the three cases all the simulations were performed with only the discrete element method (DEM) and additionally with the discrete element method (DEM) combined with computational fluid dynamics (CFD) denoted CFD-DEM. The CFD part took into account the influence and coupling of the airflow.

From the experiments the following conclusions can be drawn: With the standard air vent settings (case 1) where all the air vents were open, the experiments showed the second largest average mass in the top cavity as expected and the smallest average mass in the bottom cavity, although the average mass in the bottom cavity was only 5.1 % smaller as compared to the case with half of the air vents closed in the cavities (case 3). When 52 out of 164 of the air vents were blocked in the chamber (case 2) it gave an enhanced local air flow through the cavities and as expected the mass in the two cavities were largest with at least 21.2 % difference from the other cases. With half of the air vents blocked in the cavities (case 3), the smallest average mass in the top cavity was observed and the second smallest average mass in the bottom cavity was observed. Thus, the local air flow can be controlled e.g. by blocking air vents in the chamber and therefore increasing the local air flow through the air vents placed in the cavities as done in case 2. Decreasing the number of air vents in the cavities as done in case 3 decreased the deposited mass of green sand in the cavities as compared to case 2.

From the simulations the following conclusions can be drawn: With the chosen particle flow rates and particle velocities it was possible to simulate the deposited mass of green sand in the cavities and the qualitative flow behaviour. Larger inlet velocities for the DEM particles increased the final mass in the cavities.

The CFD-DEM simulations show larger masses in the cavities than the experimental results due to the air flow in the simulations still drags the particles into the cavities at the end of the sand shot. The side air vents could not be simulated due to the running time of the number of DEM particles when simulating a larger part of the chamber and thereby the volume of air that exits the cavities is correspondingly overestimated. In case 3 the CFD-DEM simulations were in better agreement with the selected experiment due to the lower air inlet pressure in the simulations which gave subsequently lower air velocities through the cavities.

Predictions of the mass of the green sand in the cavities were obtained with good agreement by the DEM simulations however with a tendency to underestimate the mass.

The CFD-DEM simulations predict the cavity fillings times better as compared to the DEM simulations although the CFD-DEM simulations still show too long filling times for the cavities as compared to the experiments. The results indicate that it is important to include the influence of the air flow in pneumatic transport of granular material including the 2-way coupling between the phases.

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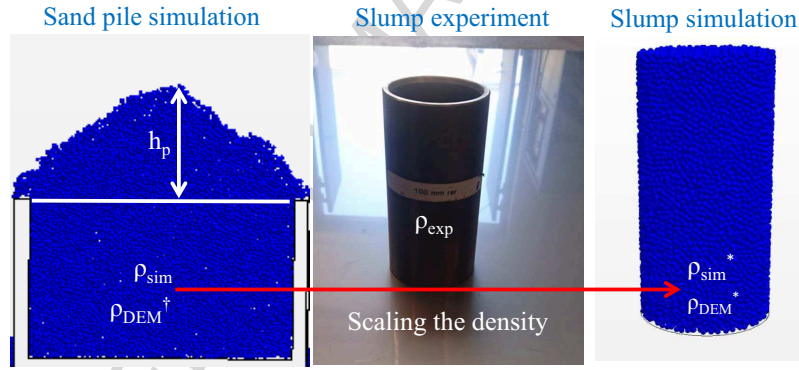


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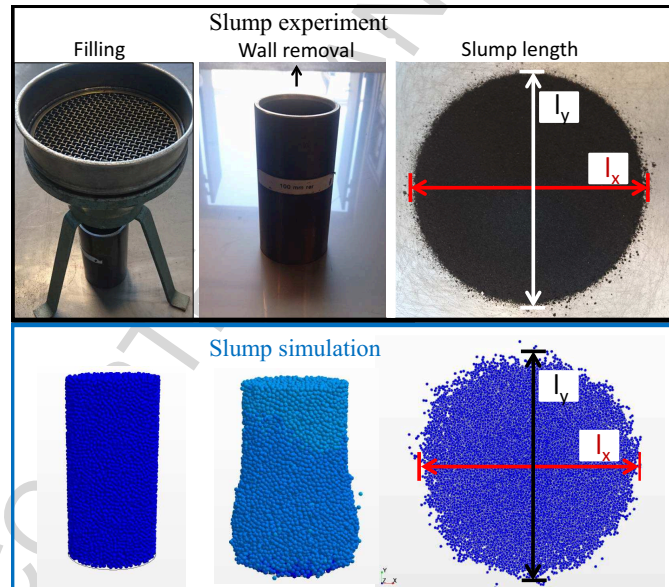


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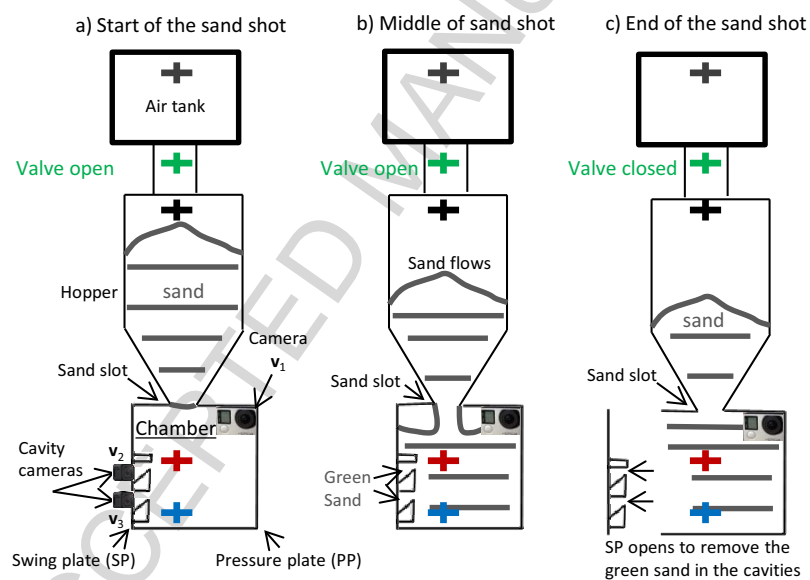


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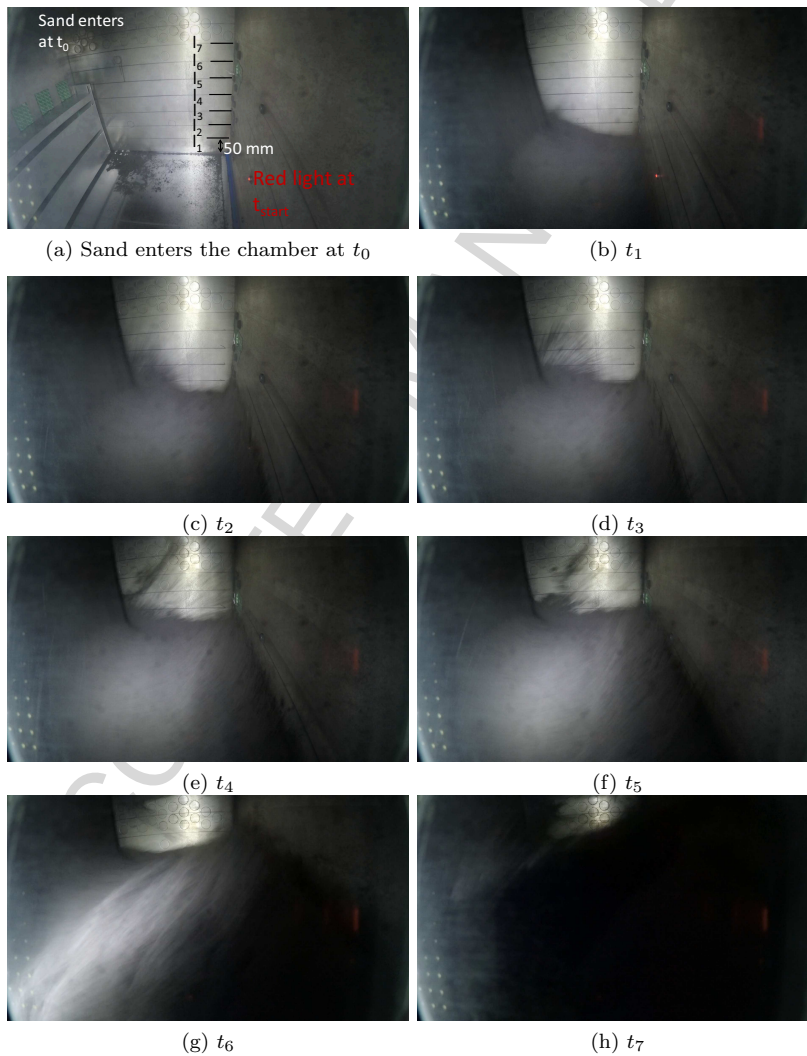


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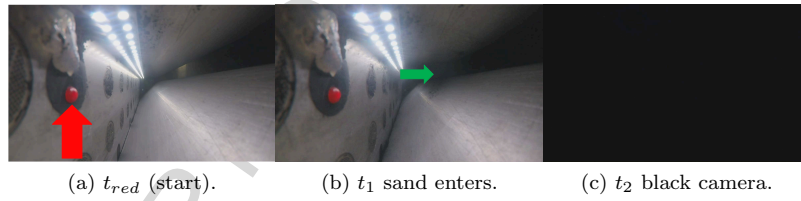


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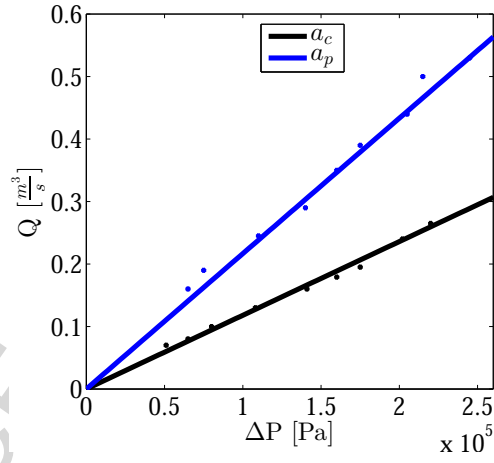


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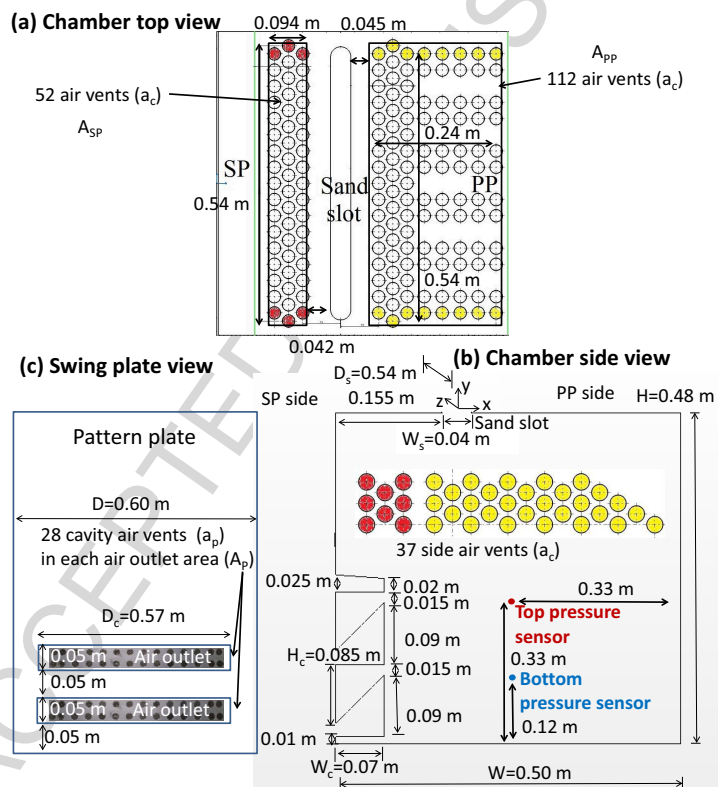


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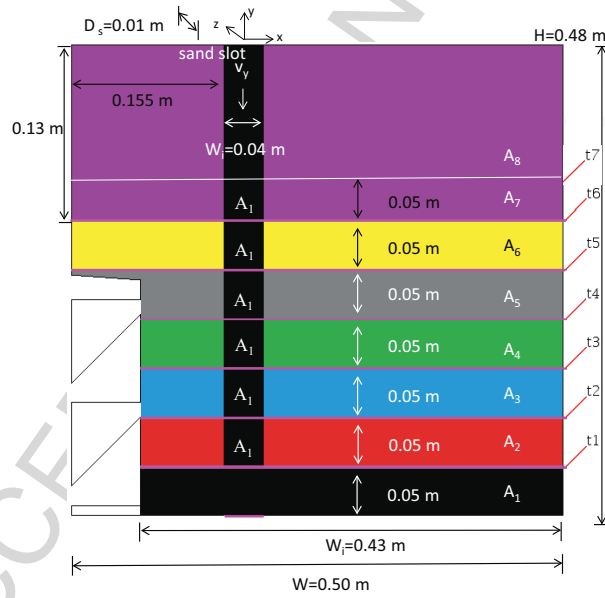


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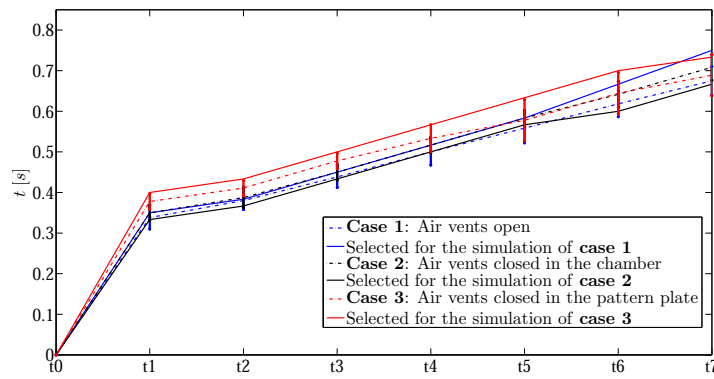


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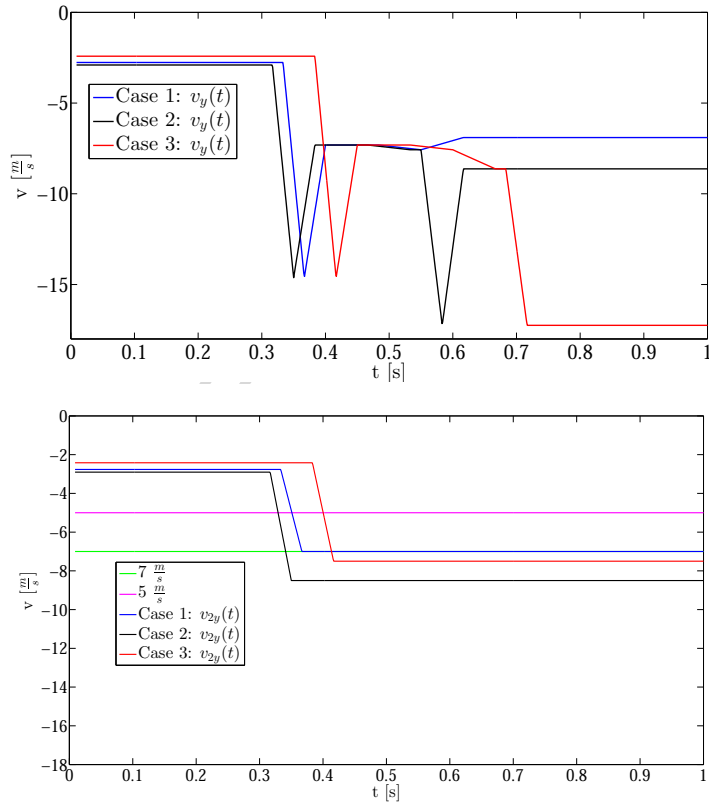


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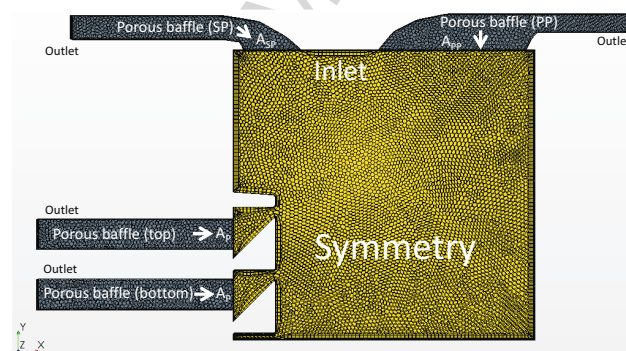


Figure 11: Placements of the boundaries.

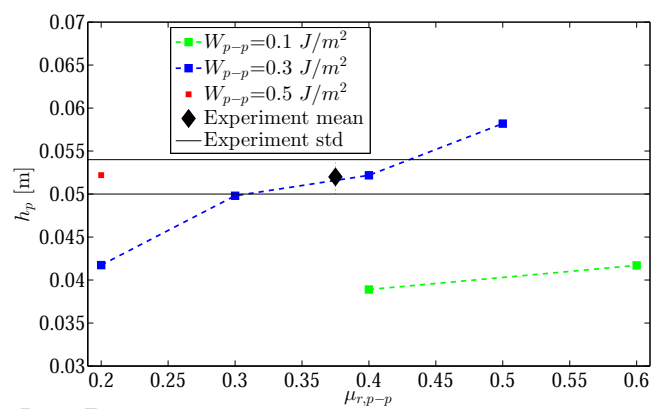


Figure 12: The black diamond is the mean height of the green sand pile experiment of $0.054 \text{ m} \pm 0.002 \text{ m}$ (black horizontal lines).

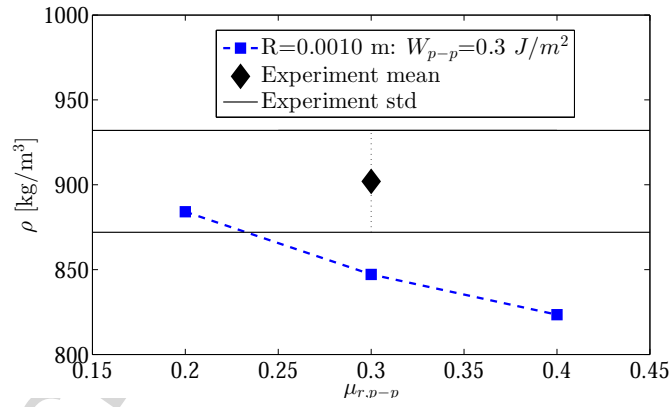


Figure 13: Plot of the density: The black diamond is the mean density of the green sand pile experiment of $902 \pm 30 \frac{kg}{m^3}$ (thin black line). The DEM simulations were made for the settings for the cohesion value $W_{p-p} = 0.3 \frac{J}{m^2}$ (blue dotted line).

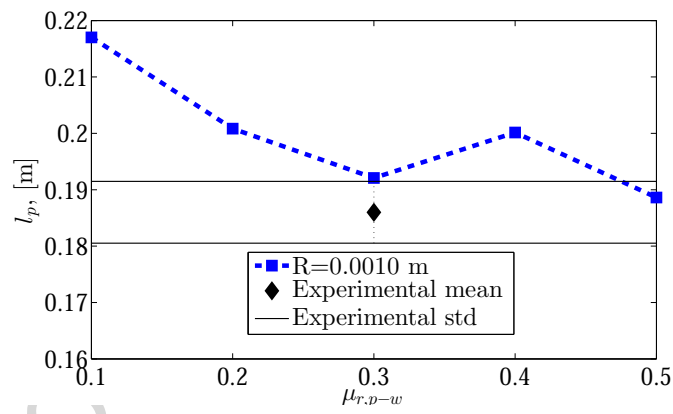


Figure 14: The black diamond is the mean length (diameter) of the green sand slump experiment of 0.186 ± 0.0548 m with the standard deviation of $\sigma = 5.48$ mm (thin black line).

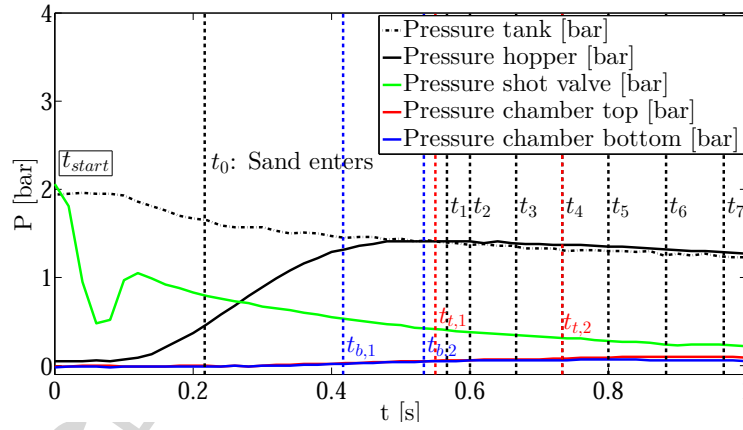


Figure 15: Example from Case 1: The pressure as a function of time is shown in the positions listed from the top to the bottom: The air tank (black dotted line), the shot valve (green), the hopper (black line), the top of the chamber (red line) and the bottom of the chamber (blue line). The atmospheric pressure is used as the reference pressure. The filling times $t_0 - t_7$ in the chamber from the chamber camera v_1 (black dotted lines).

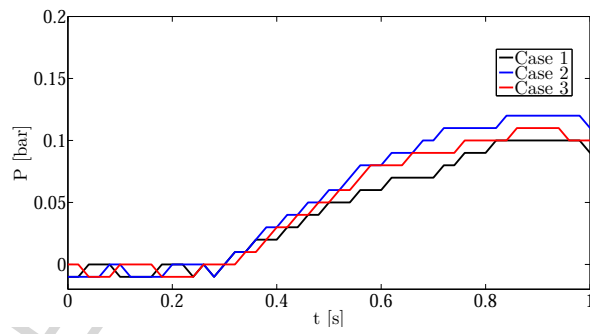


Figure 16: The three cases of experimental pressures measured at the top of the chamber as a function of time with the initial starting time of $t_0 = 0.0$ s. The atmospheric pressure is used as the reference pressure.

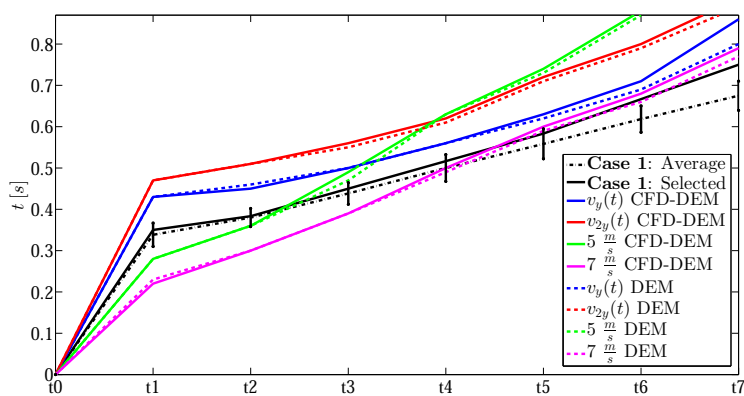


Figure 17: The experimental and simulation filling times of $t_0 - t_7$ for case 1.

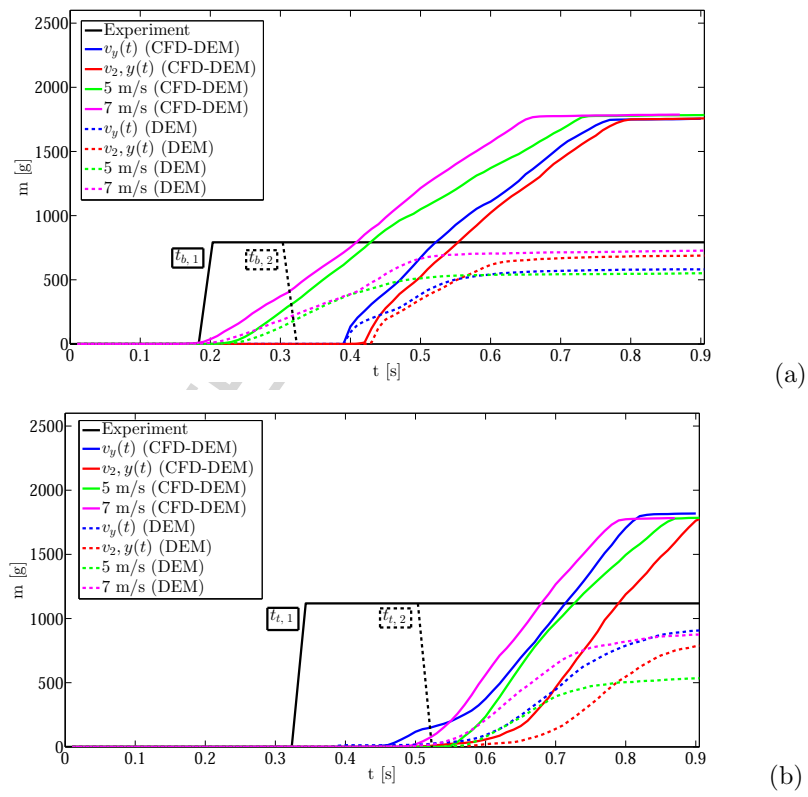


Figure 18: Case 1: The mass as a function of time for the bottom cavity (a) and for the top cavity (b).

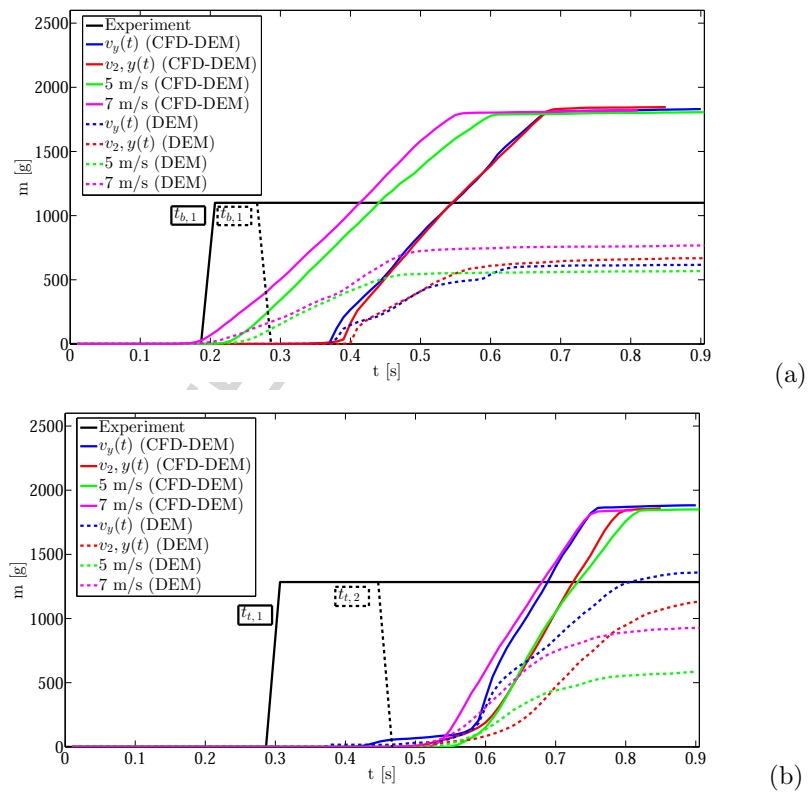


Figure 19: Case 2: The mass as a function of time for the bottom cavity (a) and for the top cavity (b).

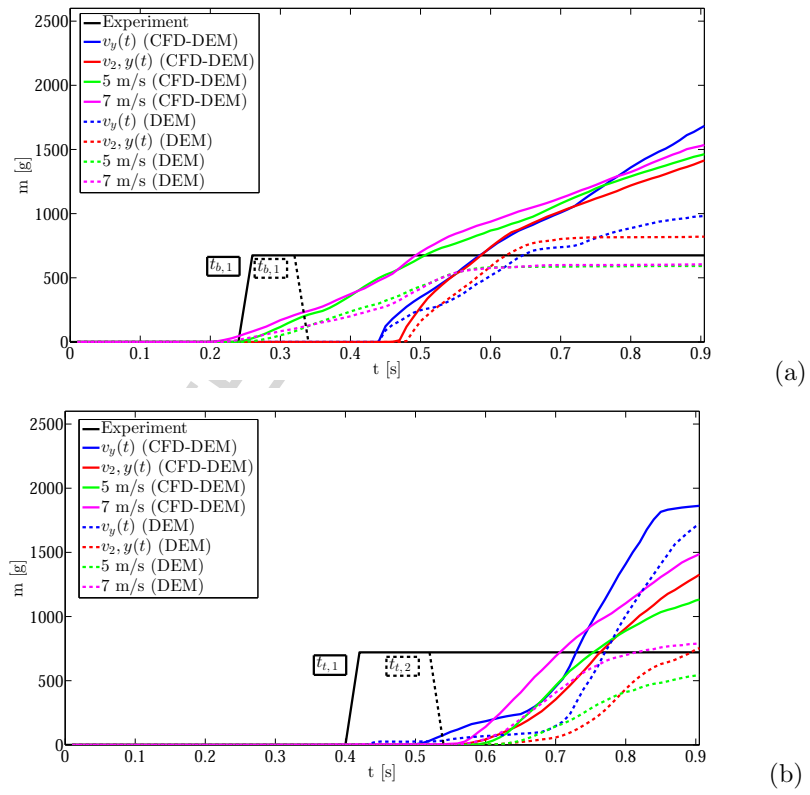


Figure 20: Case 3: The mass as a function of time for the bottom cavity (a) and for the top cavity (b).

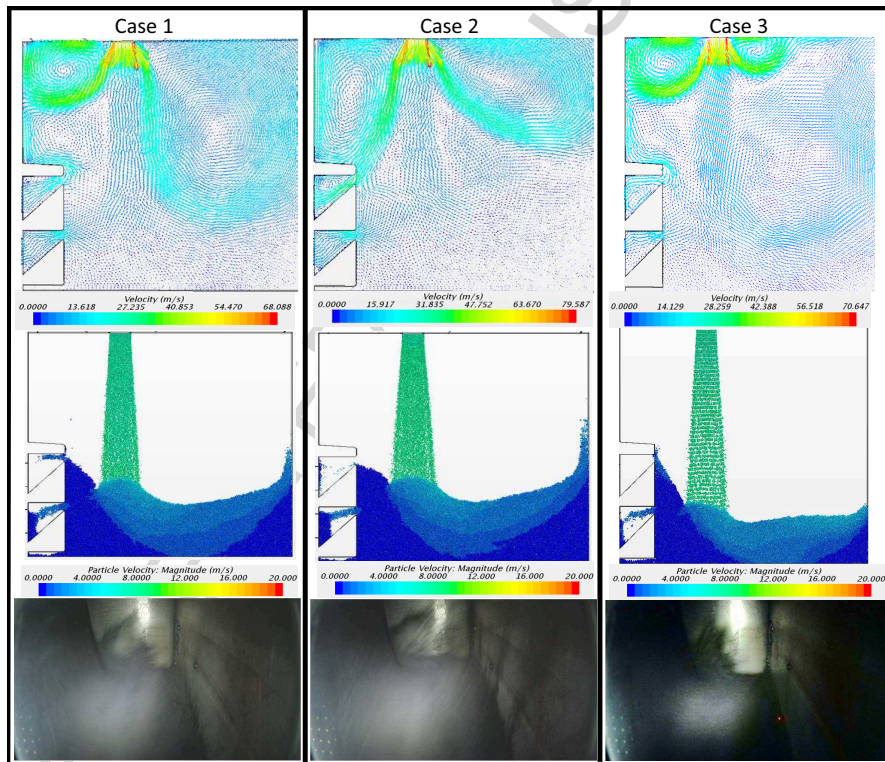


Figure 21: For the selected three cases: The time dependent velocity $v_y(t)$ simulation at time $t=0.50$ s. (Top) The velocity of the air phase. (Middle) The velocity of the particles. (Bottom) The experimental video footage at time $t=0.50$ s.

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Table 1: The experimental air vents settings in the chamber for the three cases. In case 2, 62 air vents of the type a_c are blocked in the chamber. Case 3, 14×2 air vents of the type a_p are blocked in each cavity on the pattern plate.

Case	1	2	3
SP top air vents opened (a_c)	52	0	52
PP air vents, opened (a_c)	112	112	112
Pattern plate air vents opened (a_p)	2×28	2×28	2×14
Side air vents opened, (n)	2×37	2×32	2×37
Total opened air vents ($a_c + a_p$)	294	232	266
Experimental repetitions	7	3	3

Table 2: Simulating of the air vent's settings in the chamber for the three cases. (a) Two sets of air vents are placed on the pattern plate, one in each cavity.

Case	1	2	3
SP air vents, (n)	52	0	52
A_{SP} , [m^2]	507.6×10^{-4}	No	507.6×10^{-4}
β_{SP} , [$\frac{m}{s}$]	766.2	No	766.2
PP air vents, (n)	112	112	112
A_{PP} , [m^2]	1296×10^{-4}	1296×10^{-4}	1296×10^{-4}
β_{PP} , [$\frac{m}{s}$]	908.3	908.3	908.3
Pattern plate ^a , (n)	28	28	14
A_p , [m^2]	285.0×10^{-4}	285.0×10^{-4}	142.5×10^{-4}
β_p , [$\frac{m}{s}$]	435.0	435.0	435.0

Table 3: Results from the test of the green sand calibrating the model.

Material property	average	std	Rep.
Static friction coefficient $\mu_{s,p-p}$	0.57	± 0.04	90
Static friction coefficient $\mu_{s,p-p}$	0.33	± 0.02	26
Sand pile height h_p	52×10^{-3} m	2×10^{-3} m	15
Density ρ_{Bulk}	$902 \frac{\text{kg}}{\text{m}^3}$	$\pm 30.0 \frac{\text{kg}}{\text{m}^3}$	27
Slump length l_p	186×10^{-3} m	5.48×10^{-3} m	25
Compactability	36 %	± 2.1 %	27
Water content %	3.5 %	± 0.2 %	42

Table 4: General material values for all the simulations.

Material property	Value
DEM particle radius, (R)	0.001 m
Solid density of the chamber wall (ρ_{wall})	7500 kg/m ³
Youngs modulus of the green sand, (E_p)	17000 MPa
Youngs modulus of the chamber wall, (E_w)	200000 MPa
Poisson ratio of the green sand, (ν)	0.3
Poisson ratio of the chamber wall, (ν)	0.3
Coefficient of restitution particle-particle, (e_n)	0.01
Coefficient of restitution particle-wall, (e_t)	0.01
Gravity (g)	9.82 $\frac{m}{s^2}$
Particle-wall static friction, ($\mu_{s,p-w}$)	0.33
Particle-particle static friction, ($\mu_{s,p-p}$)	0.57
The simulation time step, (Δt)	10 ⁻⁵ s

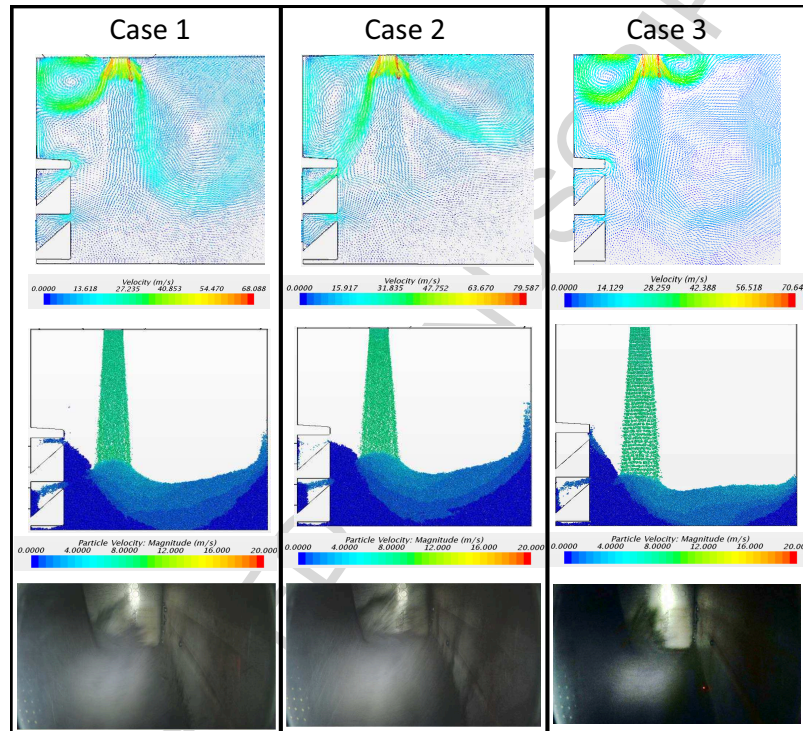
Table 5: The calibrated DEM model for simulating the DISAMATIC process.

Material property	Value
Particle-particle rolling friction coefficient ($\mu_{r,p-p}$)	0.4
Particle-particle cohesion work (W_{p-p})	$0.3 \frac{\text{J}}{\text{m}^2}$
Particle density ρ_{DEM}^*	$1900 \frac{\text{kg}}{\text{m}^3}$
Particle-wall rolling friction coefficient ($\mu_{r,p-w}$)	0.5
The simulation time step, (Δt)	10^{-4} s

Table 6: (left) Masses in the two cavities from the three cases together with the selected experiments. (right) The compactability test results from the three cases.

Case	Rep.	Bottom cavity [g]	Top cavity [g]	Rep.	ρ_{sand} [kg/m ³]
1	7	593±189	961±237	18	920±50.1
1	Selected for simulation	792	1118		
2	3	933±215	1220 ±72.5	9	970±19.7
2	Selected for simulation	1100	1284		
3	3	623±47.7	687±30.2	9	937±28.6
3	Selected for simulation	674.8	721		

Graphical abstract



- The DISAMATIC process and the geometry with the two specially designed cavities for the simulation and the experiment.
- Case 1, case 2 and case 3 for the simulated air flow (top row), the simulated granular flow (middle row) and the experimental flow profile (bottom row).

Highlights

- The calibration of the DEM model was performed with several experiments.
- A special cavity geometry was designed for investigating the locally deposition of green sand during the DISAMATIC process.
- Comparing the dynamics of the granular flow process to DEM and CFD-DEM simulations.